

B:(10 pts) Cross Product

Consider the two vectors: $\vec{U} = 3\hat{i} - 2\hat{j}$, and $\vec{V} = 6\hat{i} + 4\hat{j}$. Find their cross product $\vec{W} = \vec{U} \times \vec{V}$, and the angle θ_{UV} between them.

•(2pts) $W_x =$ _____

•(2pts) $W_y =$ _____

•(2pts) $W_z =$ _____

•(4pts) $\theta_{UV} =$ _____ (accurate to $.01^\circ$)

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•(2pts) $W_x = \underline{0}$

•(2pts) $W_y = \underline{0}$

•(2pts) $W_z = \underline{24}$

•(4pts) $\theta_{UV} = \underline{67.38^\circ}$ (accurate to .01°)

$$U = \sqrt{3^2 + (-2)^2} = \sqrt{13}$$

$$V = \sqrt{6^2 + 4^2} = \sqrt{52}$$

$$W = 24$$

$$\begin{aligned}\vec{U} \times \vec{V} &= (3\hat{i} - 2\hat{j}) \times (6\hat{i} + 4\hat{j}) \\ &= 0 + 12\hat{k} + (-12)(-\hat{k}) + 0 \\ &= \underline{24\hat{k}}\end{aligned}$$

$$W = UV \sin\theta \implies \sin\theta = \frac{W}{UV} = \frac{24}{\sqrt{676}} = \frac{24}{26}$$

$$\theta = \underline{67.3801^\circ}$$